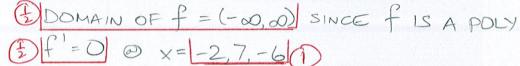
f(x) is a polynomial function

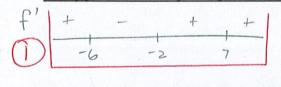
SCORE: /6 PTS

with derivative  $f'(x) = (x+2)(x-7)^2(x+6)^3$  and second derivative  $f''(x) = 6(x^2-10)(x-7)(x+6)^2$ .

Find the critical numbers of f. Justify your answer very briefly. [a]



[b] Run the First Derivative Test for Local Extrema on each critical number, and state what it tells you about that critical number. Justify your answer very briefly. Do NOT use the Second Derivative Test.

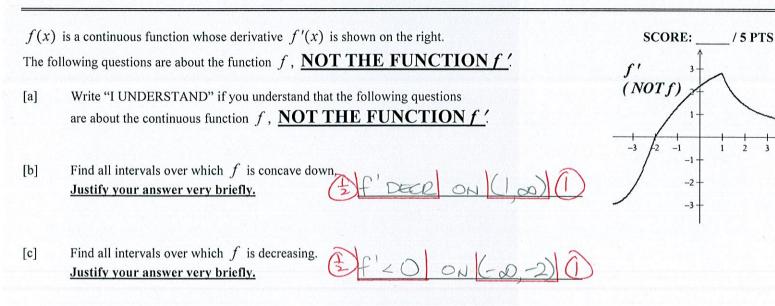


- + + f'CHANGES FROM + TO -, SO LOCAL MAX @ -6, (2)

- + LOCAL MIN @ -2, (2)

DOES NOT CHANGE SIGN, SO NO LOCAL DESTREMA (2)

Run the Second Derivative Test for Local Extrema on each critical number, and state what it tells you about that critical number c Justify your answer very briefly. Do NOT use the First Derivative Test.



[d] Find the x – coordinates of all local extrema of f and identify whether they are local maxima or minima.

Justify your answer very briefly.

SO LOCAL MIN  $\textcircled{O} \times = -2$ 

Graph  $f(x) = 25x^{\frac{3}{5}}(x+8)$  using the process shown in lecture and in the website handout.

SCORE: / 19 PTS

Complete the table at the bottom of the page, after showing relevant work (you do NOT need to show work for entries marked ★). You will NOT receive credit for the entries in the table if the relevant work is missing.

y-INT: f(0)=25(0)(8)=0

X-INT: 25x3 (x+8)=0 → X=0 ORX=-8

lim 25x3 (x+8) = 00 (00.00) (2) POINT

1:m 25x3(x+8)= 00 (-0.-00) WALESS

 $f(x) = 25 \times \frac{8}{5} + 200 \times \frac{3}{5}$ 

f(x)= 40x= +120x== +0x==(x+3)

f"(x)=24x-3-48x-3= 24x-3(x-2)

F' DREW X=0 | F" DREW X=0

| 2 | <b>★</b> Domain                           | ★ Discontinuities                           | Intercepts (specify $x - \text{ or } y - $ ) | One sided limits at each discontinuity (write using proper limit notation) |                                      |  |
|---|---|---|--|--|--------------------------------------|--|
|   | (-00,00)                                  | NONE  | X-INT: -8, 0,<br>Y-INT: 0                    | N/   | N/A                                  |  |
|   | Equations of<br>Horizontal Asymptotes     | Intervals of Increase                       | Intervals of Decrease                        | Intervals of Upward<br>Concavity   | Intervals of Downward<br>Concavity   |  |
|   | MONE                                      | (-3,00)                                     | $(-\infty, -3)$                              | (-0,0)(2,0)  | (0,2)                                |  |
|   | Vertical Tangent<br>Lines (x-coordinates) | Horizontal Tangent<br>Lines (x-coordinates) | Local Maxima (x-coordinates)                 | Local Minima<br>(x-coordinates)  | Inflection Points<br>(x-coordinates) |  |
|   | X=O                                       | x=-3  | NONE   | X=-3   | x=2                                  |  |